

Cryptanalysis of a Hash Function Based on Quasi-Cyclic Codes

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Hash Functions

$$F : \{0, 1\}^* \mapsto \{0, 1\}^n$$

Should behave “like a random oracle”...

Collision attack

Given F , find $M_1 \neq M_2$ s.t. $F(M_1) = F(M_2)$.

Ideal security: $2^{n/2}$.

Second-preimage attack

Given F and M_1 , find $M_2 \neq M_1$ s.t. $F(M_1) = F(M_2)$.

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Preimage attack

Given F and \bar{H} , find M s.t. $F(M) = \bar{H}$.

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Hash Function Design

Most hash functions are dedicated designs based on *symmetric crypto* concepts:

e.g. MDx, SHA-x, Whirlpool, RadioGatún, Grindahl, ...

Some designs are based on a provable security approach: the security relies on a given hard problem (like *public key crypto*):

e.g. FSB, LASH, SWIFFT, SQUASH, ...

Proof of security should be taken with caution

- ▶ Many of them are asymptotic proofs but the concrete function has a fixed size.
- ▶ Reduction to an NP-complete problem means that *some* instance are hard, but the fixed instance could be easy.
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Hash Function Cryptanalysis

Many hash functions in use today are broken:

1990 MD4 design (Rivest)

1992 MD5 design (Rivest)

1995 SHA-1 design (NIST)

1996 MD4 collisions (Dobbertin)

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2004 MD5 collisions (Wang *et al.*)

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Best collision attacks

MD4 Complexity 2^1 (Wang *et al.* – Sasaki *et al.*)

MD5 Complexity 2^{22} (Wang *et al.* – Klima)

SHA-1 Complexity $2^{60.x}$ (Wang *et al.* – Rechberger *et al.*)

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The IFSB Hash Function

Description

Previous cryptanalysis

Wagner's Generalized Birthday

Linearization Attack

The Cyclic attack

Using Periodic Messages

Description of the attack

Solving the cyclic equations

Scope of the attack

Description of FSB

$\mathbf{x} = 1 \ 1 \ 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 1 \ 1$

$$F(x) = \mathcal{H} \times \varphi(x)$$

\mathcal{H} : random $r \times n$ matrix

φ : encodes s bits to n bits with weight w

Description of FSB

$$x = \begin{array}{|c|c|c|c|c|c|c|c|c|c|} \hline 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ \hline \end{array}$$

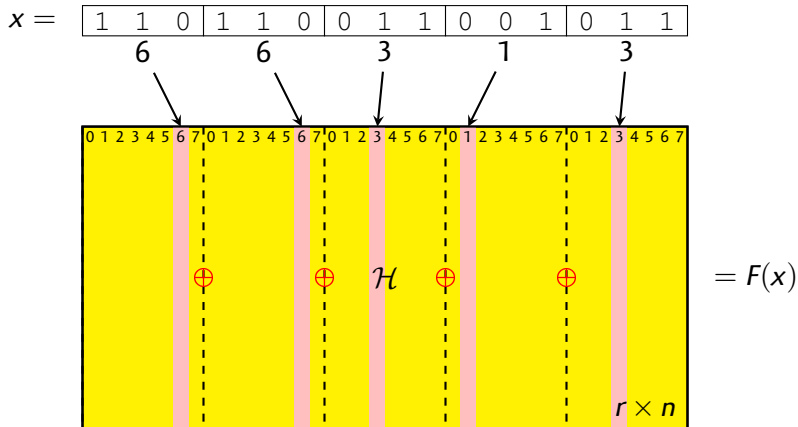
6
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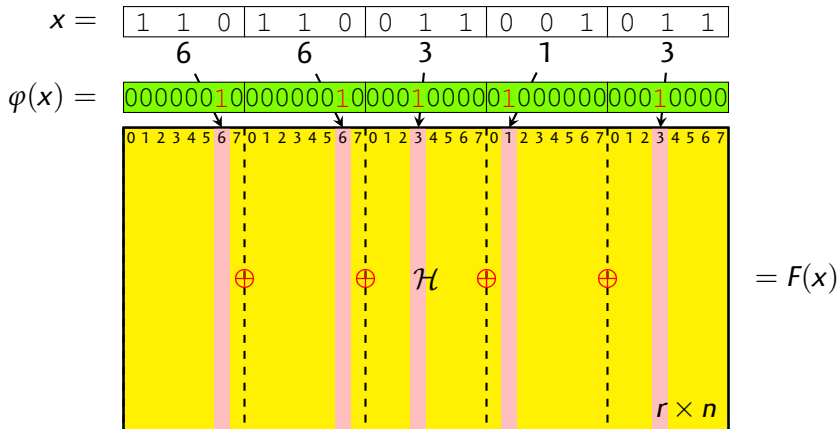


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Rationale of FSB

$$F(x) = \mathcal{H} \times \varphi(x)$$

\mathcal{H} : random $r \times n$ matrix

φ : encodes s bits to n bits with weight w

- ▶ \mathcal{H} is the parity matrix of a linear code.
- ▶ $\varphi(x)$ is an error pattern.
- ▶ $\mathcal{H} \times \varphi(x)$ is a syndrome.
- ▶ Inversion and collision are related to coding theory problems (syndrome decoding) on \mathcal{H} .

From FSB to IFSB

- ▶ Main problem: the matrix \mathcal{H} is huge...
- ▶ Use a quasi-cyclic matrix:

$$\mathcal{H} = \left[\begin{array}{ccccc|ccccc|c} \alpha_0 & \alpha_1 & \dots & \alpha_{r-2} & \alpha_{r-1} & \beta_0 & \beta_1 & \dots & \beta_{r-2} & \beta_{r-1} & \\ \alpha_{r-1} & \alpha_0 & \alpha_1 & & \alpha_{r-2} & \beta_{r-1} & \beta_0 & \beta_1 & & \beta_{r-2} & \\ \vdots & \alpha_{r-1} & \alpha_0 & \ddots & \vdots & \vdots & \beta_{r-1} & \beta_0 & \ddots & \vdots & \dots \\ \alpha_2 & & \ddots & \ddots & \alpha_1 & \beta_2 & & \ddots & \ddots & \beta_1 & \\ \alpha_1 & \alpha_2 & \dots & \alpha_{r-1} & \alpha_0 & \beta_1 & \beta_2 & \dots & \beta_{r-1} & \beta_0 & \end{array} \right]$$

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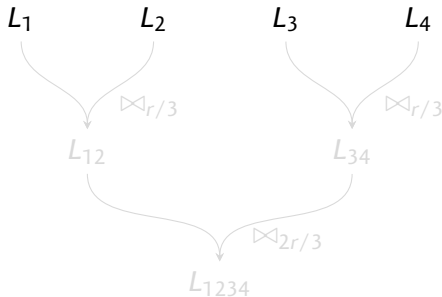
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Wagner's Generalized Birthday

- ▶ Solves the k -sum problem:
find $l_1 \in L_1, \dots, l_k \in L_k$ s.t. $\bigoplus_{i=1}^k l_i = 0$.
- ▶ $L \bowtie_j L' = \{(l, l') \in L \times L' \mid (l \oplus l')^{[0..j-1]} = 0^j\}$.
- ▶ For r bits, start with 2^a lists of $2^{r/(a+1)}$ elements.



4 lists of $2^{r/3}$ elements

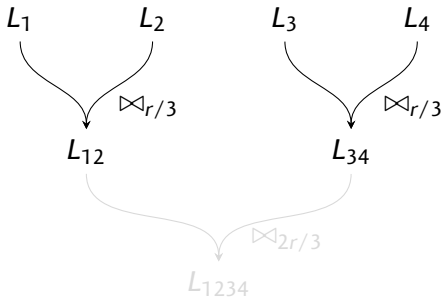
2 lists of $2^{r/3}$ elements
with $2^{r/3}$ zeros

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- ▶ One element in L_{1234} is zero.
- ▶ Complexity: 7 sorts.

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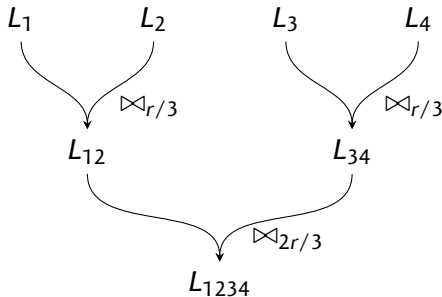
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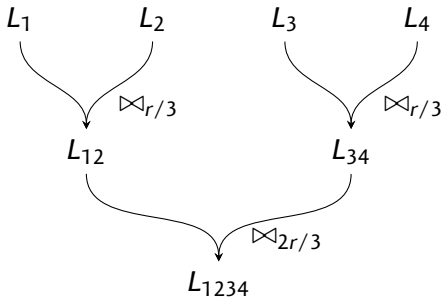
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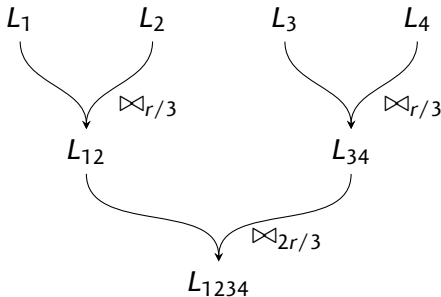
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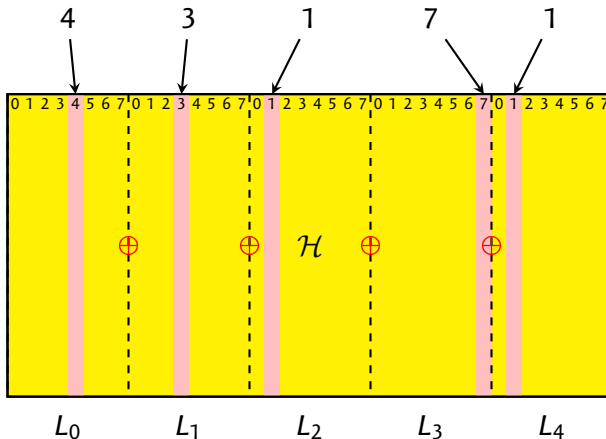
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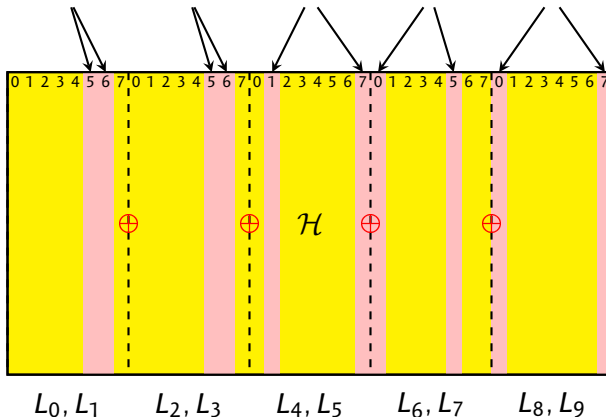
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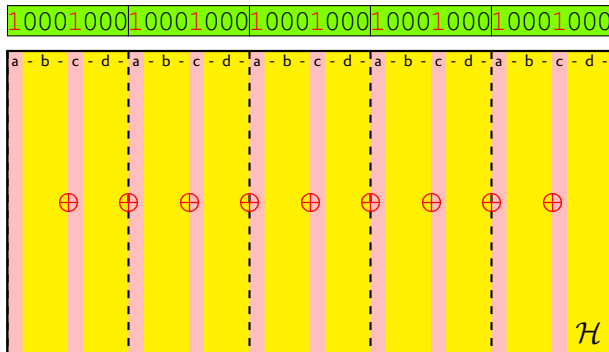
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Linearization Attack

- ▶ Choose a, b, c, d . Start with $x = a^w$ and $x' = c^w$.

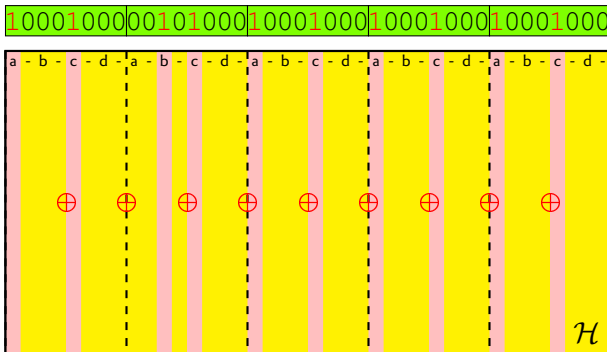


$$= F(a^w) \oplus F(b^w)$$

- ▶ Each a can be changed to b . And c to d .
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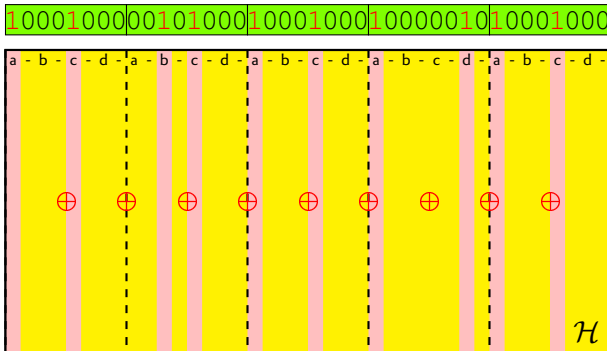


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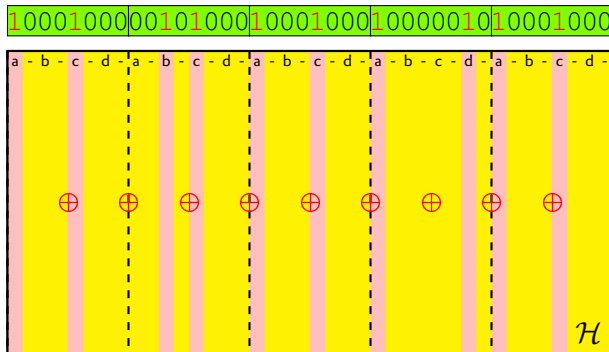


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Linearization attack against IFSB

- ▶ We reduce the message space: $x \in \{ab\}^*$, $x' \in \{cd\}^*$.
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State of the art

- ▶ The original FSB needs a huge matrix and is slow
- ▶ The parameters of IFSB are bad
- ▶ No structural attack against IFSB
- ▶ No attack known if r/w is big enough

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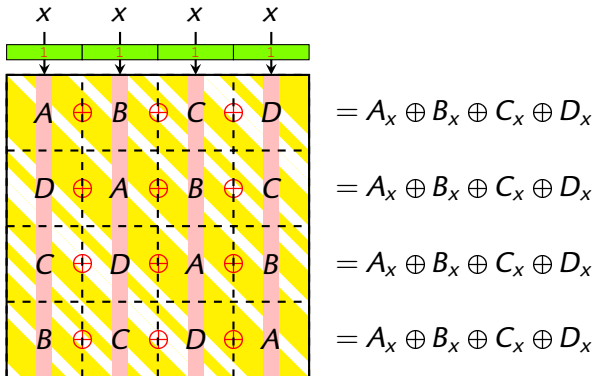
Solving the cyclic equations

Scope of the attack

Cyclic code and periodicity

Property

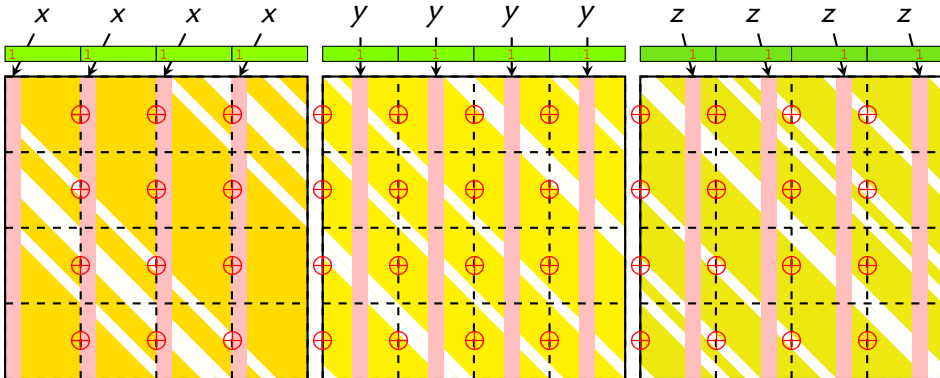
If \mathcal{H} is cyclic and $\varphi(M)$ is periodic,
then $\mathcal{H} \times \varphi(M)$ is periodic.



Quasi-cyclic code and periodicity

Property

If \mathcal{H} is quasi-cyclic and $\varphi(M)$ is piecewise-periodic, then $\mathcal{H} \times \varphi(M)$ is periodic.



The Periodic attack

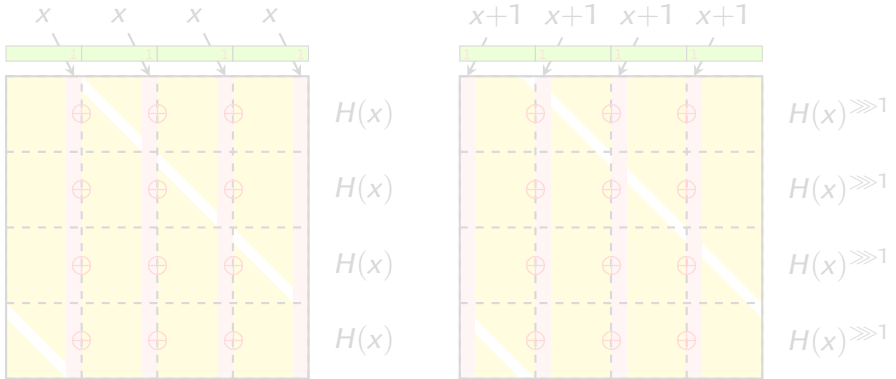
Basic idea of the attack

- ▶ Use a piecewise-periodic $\varphi(M)$
 - ▶ Cancel **one period** of the output.
-
- ▶ We can use Wagner's attack to cancel one period.
 - ▶ a' is a or $a - 1$, but smaller matrix:

Attack	Complexity	Remarks
Wagner	$r2^{a'} \cdot 2^{r/(a+1)}$	r is typically 1024
Cyclic + Wagner	$\frac{n}{2w} 2^{a'} \cdot 2^{\frac{n}{2w}/(a'+1)}$	$n/4w$ is typically 128

The Cyclic attack

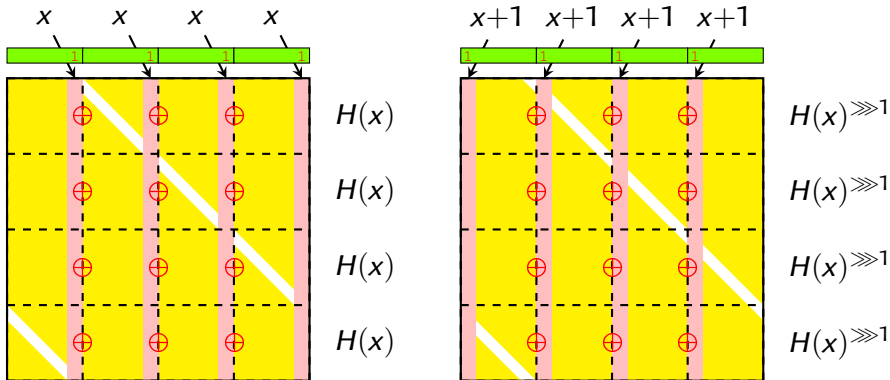
- ▶ Is there some more structure that we can use?
- ▶ Yes: for each cyclic block, the outputs are still related:



- ▶ Collision iff $\bigoplus_{i=0}^{p-1} H_i \lll \mu_i = 0$

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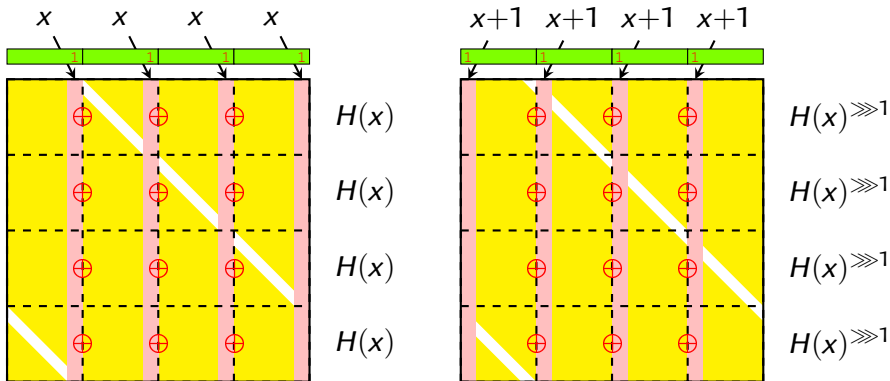
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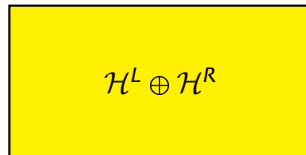
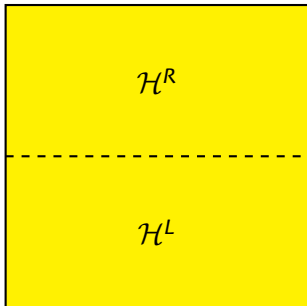
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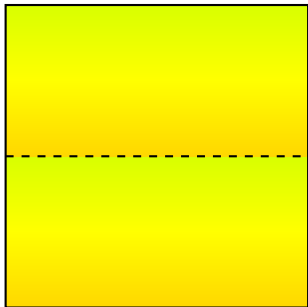
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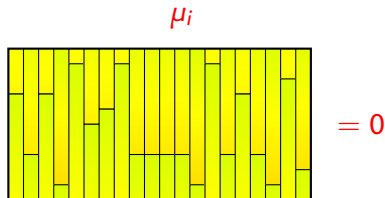
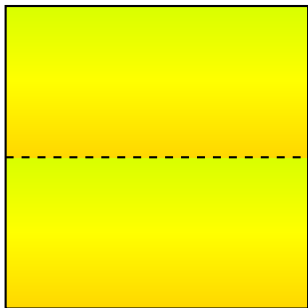
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- ▶ Solve for $\mathcal{H}^L \oplus \mathcal{H}^R$
- ▶ Apply the rotation to \mathcal{H}
- ▶ The MSB of μ_i exchanges H_i^L and H_i^R
- ▶ Linear system for $\bigoplus H_i^L \lll \mu_i = 0$
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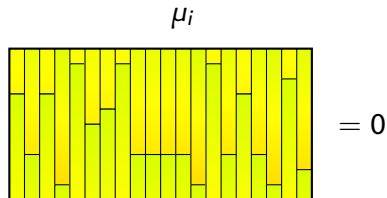
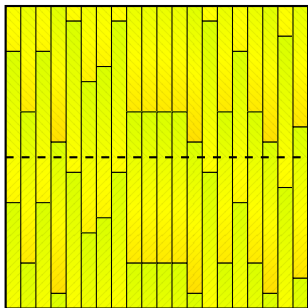
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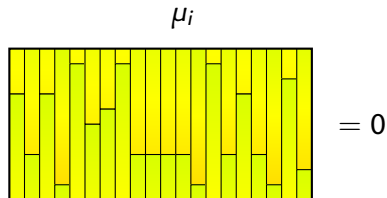
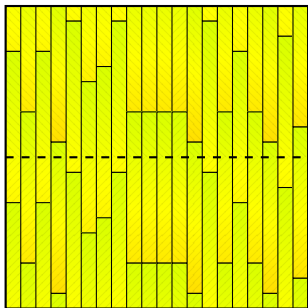
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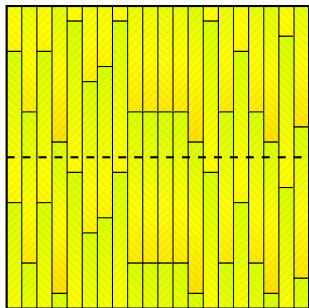
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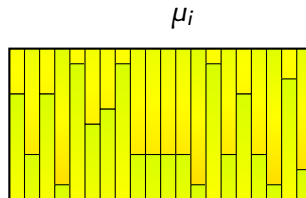


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$$\mu_i \text{ Solve } \bigoplus_{i=0}^{p-1} H_i \lll \mu_i = 0$$



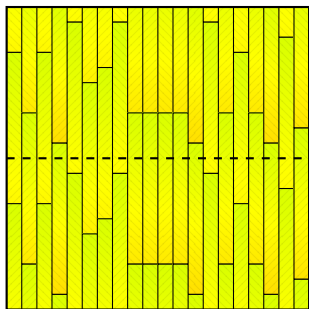
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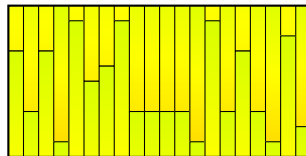
- ▶ $\mathcal{H} = \mathcal{H}^L || \mathcal{H}^R$
- ▶ Solve for $\mathcal{H}^L \oplus \mathcal{H}^R$
- ▶ Apply the rotation to \mathcal{H}
- ▶ The MSB of μ_i exchanges H_i^L and H_i^R
- ▶ **Linear system for $\bigoplus H_i^L \lll \mu_i = 0$**
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Overview

The full attack looks like periodic + linearization.

Linearization attack

Conditions	Complexity	Remarks
$r \leq 2w$ if r is bigger	r^3 $(4/3)^{r-2w} \cdot r^3$	r is typically 1024 $\log_2(4/3) \approx 0.415$

Cyclic attack

Conditions	Complexity	Remarks
$r \leq 4w$ if r is bigger	$(n/4w)^3$ $2^{\frac{n(r-4w)}{4wr}} \cdot (n/4w)^3$	$n/4w$ is typically 64 $n/4wr$ is typically 1/16

Scope of the Attack

In this talk, we assume that all the parameters are powers of 2.

- ▶ We need a small divisor d of r for the periodic attack.
- ▶ d must be a power of 2 for the cyclic attack.

Actually one of the parameter set of IFSB uses a prime r ...

This is due to a result about quasi-cyclic codes:

Theorem

*If r is a prime such that 2 is primitive modulo n ,
Then the matrix generated by a word of odd weight is invertible,
and the code has the same kind of properties than a random code.*

This does not prove the security of IFSB with a good r ...

Our attack complements this result:

if r has a small divisor, it is easy to invert periodic syndromes.

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On Provable Security

Regular Syndrome Decoding is NP-hard but...

- ▶ There is an efficient algorithm for small matrix:
Wagner attack.
- ▶ It is easy when $r \leq 2w$: *linearization attack.*

Quasi-Cyclic Regular Syndrome Decoding is hard but...

- ▶ For some parameters, it is easy to decode a periodic syndrome: *cyclic attack.*

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IFSB Status

- ▶ The original FSB needs a huge matrix and is slow
- ▶ The parameters of IFSB are really bad
- ▶ **Structural attack against IFSB with a bad r**
- ▶ No attack known if r is carefully chosen and r/w is big enough

Any Questions?

Thank you for your attention.